# The scale effect analysis of slope length based on DEM multi-scale representation

Weiling Guo<sup>1</sup>, Qinke Yang<sup>2</sup>, Haijiang Wang<sup>3</sup>, Rui Li<sup>4</sup>

 Anhui University of Science & Technology,
Huainan, Anhui, 232001; 2. College of Urban and Environment, Northwest University, Xi' an,

ABSTRACT: It's the only way to extract slope gradient and slope length based on low-resolution DEMs for the studies of regional scale soil erosion modeling. But the slope gradient will reduce and the slope length will enlarge. In Xiannangou catchment, a database of DEM is established by using the wavelet multi-resolution analysis method, which has a gradually-changing resolution and a unified position control base, and effective ability in representing the overall topographic characteristics and landform macro structure. On this basis, we deeply reveal that the variation pattern of the slope length increases as the DEM resolution becomes coarser. The results show that, with DEM resolution become coarser, the gully elevation is rising, while the Liang and Mao top elevation are decreasing, and the small-scale gully, Liang and Mao top are gradually disappeared. Average slope length has a linearly increasing trend with the reduction of DEM resolution, and slope length cumulative frequency curve is moving towards larger value. In general, the overall slope length is enlarged, and the enlarging mainly happens in the middle and bottom of slopes.

*Keywords:* DEM multi-scale representation, wavelet multi-resolution analysis, slope length increase, scale effect of slope length

# INTRODUCTION

Slope gradient and slope length are two of the most important terrain indexes which influence soil erosion<sup>[1]</sup>. These two indexes are normally extracted from DEMs with lower resolution in the research of regional soil erosion. 710069, 3. Hebei University of Engineering, Handan, Hebei, 056038; 4. Institute of Soil and Water Conservation Chinese Academy of Sciences Ministry of Water Resources, Yangling, Shaanxi, 712100)

However, slope gradient tends to decreas<sup>e[2-8]</sup> and slope length tends to increase<sup>[9]</sup> as resolution becomes coarser. These make the calculated slope gradient and slope length not accurate enough to describe the real relief of terrain. Thus the accuracy of hydrology and soil erosion model is declined<sup>[8, 10, 11]</sup>. At present, the studies on slope gradient decreases are more. For slope length increases, some researchers have paid attention to this phenomenon and its effect, but there are few research reports about scale effect of slope length. Therefore, it has a very important significance for regional scale soil erosion research to study on the rule and mechanism of low-resolution slope length increases.

DEM is the basic data of terrain factor extraction and digital terrain analysis and application<sup>[12, 13]</sup>. Multi-scale DEM data in the same area have become the basic DEM data source of terrain factor scale effect analysis. And wavelet analysis method with the reputation of "mathematical microscope" is a striking similarity to the basic idea of spatial data multi-scale representation which provides an effective way to analyze and express different resolution DEMs.

### METHOD

# The study area and base data

The study area locates in Xiannangou Catchment in Loess Hilly and Gully Region in the Loess Plateau. It is a square area with 25km. The area is a typical Loess Hilly-Gully area with complex terrain surface and intensively soil erosion.

The original DEM data is the

Hydrological-correct DEMs (Hc-DEMs)<sup>[14, 15]</sup> of high resolution (2.5m) generated by 1:10 000 scale digital topographic map using AUNDEM software. In addition, taking the Hc-DEM data with the resolution of 10m, 25m and 50m generated by 1:50 000, 1:100 000 and 1:250 000 scale digital topographic map as reference data. The projection is Gauss\_Kruger based on the Krasovsky 1940 Datum.

# Wavelet transform and slope length extraction

Wavelets are mathematical functions that decompose signals into different frequency components, and represent each component with a resolution matched to its scale. The elegance of the wavelet multi-resolution analysis of  $L^2(R)$ comes from the fact that the scaling functions  $\varphi$ generate a set of nested subspaces  $V_j$  of

 $L^{2}(R), j \in \mathbb{Z}$ , while the associated wavelets  $\psi$ constitute their orthogonal complementary subspaces  $W_{j}$ , i.e.  $V_{j} = V_{j+1} \oplus W_{j+1}$ . f(x) is represented with a set of orthonormal basis in  $V_{j+1}$  ( $\{\varphi_{j+1}, k \in \mathbb{Z}\}$ ) and  $W_{j+1}$  ( $\{\psi_{j+1}, k \in \mathbb{Z}\}$ ),

i.e.

$$f(x) = \sum_{n} c_{n}^{j+1} \varphi_{j+1,n} + \sum_{n} d_{n}^{j+1} \psi_{j+1,n} . \quad (1)$$

Here,

$$c_k^{j+1} = \sum_n h_{n-2k} c_n^j , \qquad (2)$$

$$d_k^{j+1} = \sum_n g_{n-2k} c_n^j \,. \tag{3}$$

That is orthogonal wavelet decomposition procedure for discrete signal. Here j are levels of wavelet decomposition;  $h_{n-2k}$  is scaling coefficients and  $g_{n-2k}$  is wavelet coefficient of a wavelet system, respectively corresponding to low-pass and high-pass filter coefficient.

Since the wavelet transform is a filtering process, it is efficient for wavelet transform to reconstruct the original signal using either de-convolution or the inverse filter. Wavelet reconstruction function is

$$c_n^{j} = \sum_{k \in \mathbb{Z}} h_{n-2k} c_k^{j+1} + \sum_{k \in \mathbb{Z}} g_{n-2k} d_k^{j+1}$$
(4)

Where  $c_k^{j+1}$  is low-frequency component;  $d_k^{j+1}$ 

is high-frequency component;  $c_n^j$  is wavelet reconstruction component;  $h_{n-2k}$  is low-pass filter coefficient of wavelet reconstruction;  $g_{n-2k}$  is high-pass filter coefficient of wavelet reconstruction.

The orthogonal wavelet decomposition and reconstruction equations are theories basis of DEM multi-scale representation when DEM is regarded as a discrete signal.

Since DEM multi-scale representation is a process of filtering partial fractal terrain, and considering such as compactly supported, symmetric, orthogonal , regularity and larger cancellation, we select biorthogonal wavelet function bior4.4. In addition, the Radical Law Selection Principles<sup>[16]</sup>, traditionally feature selection principle used in artificial cartographic generalization, was used to set different scale parameters during the threshold processing on the wavelet high frequency coefficients. i.e.

$$N_b = N_a \sqrt{M_a / M_b} \tag{5}$$

Here,  $N_a$  and  $N_b$  is respectively the number of high frequency wavelet coefficients of 2.5m resolution and derived DEM.  $M_a$  is the scale denominator of the source map;  $M_b$  is denominator of scale parameters of the derived DEM used in the implement of wavelet transform.

The calculation method of slope length is runoff accumulation algorithm based on the soil erosion principle<sup>[17]</sup>, which flow direction algorithm is used by multiple flow direction algorithms (MS)<sup>[18]</sup>.

### **RESULTS AND ANALYSIS**

A set of DEMs are established by using the

wavelet multi-resolution analysis method, which has a gradually-changing resolution and a unified position control base, and effective ability in representing the overall topographic characteristics and landform macro structure. Fig.1 shows the DEM multi-scale representation.



(a) 2.5m original DEM





(b) scale parameter 200 000



 (c) scale parameter 600 000
(d) scale parameter 1 000 000
Fig.1 DEM multi-scale representation of different scale parameters with wavelet transform

On this basis, we deeply reveal that the variation pattern of the slope length increases as the DEM resolution becomes coarser. Taking the Hc-DEM data with the resolution of 10m, 25m and 50m generated by 1:50 000, 1:100 000 and 1:250 000 scale digital topographic map using ANUDEM software in Xiannannou Catchment as reference data, the paper evaluates the quality of the generated DEMs, which have different scale parameter and obtained by using wavelet transform method using the elevation shannon, playback contours and slope gradient histogram similarity. Then, the relationship between the scale parameter and resolution is established (Fig.2). Hence, the generation of DEMs with arbitrary coarser resolutions is realized.



Fig.2 the relationship curve between DEM scale parameters after wavelet transform and DEM resolutions generated by digital topographic map

Based on the multi-resolution database obtained by using wavelet transform, the variation pattern of slope length along with the changing of DEM resolution is analyzed. The results show that with DEM resolution become coarser, the gully elevation is rising, while the Liang and Mao top elevation are decreasing, and the small-scale gully, Liang and Mao top are gradually disappeared. Average slope length has a linearly increasing trend with the reduction of DEM resolution (Fig.3). In general, the overall slope length is enlarged, and the enlarging mainly happens in the middle and bottom of slopes (Fig.4).



Fig.3 Change trend of average slope length with DEM resolution become coarser



(a) scale parameter 200 000

(b) scale parameter 400 000



Fig.4 The slope length differential map extracted by DEM of 2.5m

resolution and different scale parameter

# CONCLUSIONS

With the analyses above, we can conclude that: A database of DEM is established by using the wavelet multi-resolution analysis method, which has a gradually-changing resolution and a unified position control base. Slope length increases along with DEM resolution become coarser and the location of slope length changing is mainly in the middle and bottom of slopes.

# DISCUSSIONS

According to this study, slope length on the scale of the DEM resolution has great dependence. Therefore, In large scale range, such as regional scale, it is need to transform slope length extracted from the low resolution DEM to that of the high-resolution with higher accuracy and consistent ability to reflect the terrain relief, so that the Calculated LS factor can be applied for the regional soil erosion evaluation and it has guiding significance for the national soil erosion survey and actual soil and water conservation measures.

# ACKNOWLEDGMENT

This study has been financially supported through the projects Estimating Spatially Distributed Slope Length at Watershed for Soil Erosion Assessment (NSFC Project, 41071188) and Study on theoretical distribution model of Slope (NSFC Project, 41301284).

### REFERENCES

[1] Wischmeier, W. H. and Smith, D. D. Predicting rainfall

eosion losses from cropland east of the Rocky Mountains: A Guide for soil and water conservation planning. USDA Agriculture Handbook. 1978. 537.

[2] David, M. W. and Gregory, J. M. Differences in topographic characteristics computed from 100- and 1000-m resolution digital elevation model data. hydrological processes [J]. 2000, 14: 987-1002.

[3] Gao, J. Resolution and Accuracy of Terrain Representation by Grid DEMs at a Micro-scale. International Journal of Geographical Information Science [J]. 1997, 11(2): 199-210.

[4] James, A., Thompson, J. C. B., Charles, A., et al. Digital elevation model resolution: effects on terrain attribute calculation and quantitative soil-landscape modeling. Geoderma [J]. 2001, (100): 67-69.

[5] Wolock, D. M. and McCabe, G. J. Differences in topographic characteristics computed from 100- and 1000-m resolution digital elevation model data. Hydrological Processes [J]. 2000, (14): 987-1002.

[6] Yang, Q. K., Jupp, D., Li, R., et al., Re-scaling lower resolution slope by histogram matching, in Advances in Digital Terrain Analysis (Lecture Notes in Geoinformation and Cartograph), Q.M. Zhou, B.G. Lees, and G.A. Tang, Editors. 2008, Springer. p. 193-210.

[7] Yin, Z. Y. and Wang, X. H. A cross-scale comparison of drainage basin characteristics derived from Digital Elevation Models. Earth Surface Processes and Landforms [J]. 1999, (24): 557-562.

[8] Tang, G. A., Zhao, M. D., Li, T. W., et al. Modeling slope uncertainty derived from DEMs in Loess Plateau. Acta Geographica Sinica [J]. 2003, 58(6): 824-830.

[9] Guo, W. L., Yang, Q. K., Cheng, L., et al. Re-scaling method of slope length factor in the soil erosion a ssessment of regional scale. Science of Soil and Water Conservation [J]. 2010, 8(4): 73-78.

[10] Tang, G. A., Yang, W. Y., Qin, H. R., et al. An Application of using GIS technology to return hillside cultivated land for forestry and grassland in Loess Plateau region. Bulletin of Soil and Water Conservation [J]. 2002, 22(5): 46-50.

[11] Liu, X. H., Yang, Q. K., and Tang, G. A. Extraction and application of relief of China Based on DEM and GIS method. Bullet in of Soil and Water Conservation [J]. 2001, 21(1): 57-59, 62.

[12] Pike, R. J., Evans, I. S., and Hengl, T., Geomorphometry: a brief guide, in Geomorphometry: Concepts, Software, Applications, T. Hengl, Reuter, H. I. (eds), Editor. 2009, Amsterdam: Elsevier p. 3-30.

[13] Wilson, J. P. Digital terrain modeling. Geomorphology [J]. 2012, 137(1): 107-121.

[14] Hutchinson, M. F. A new procedure for gridding elevation and stream line data with automatic removal of spurious pits. Journal of Hydrology [J]. 1989, 106(3): 211-232.

[15] Hutchinson, M. F. ANUDEM version 5.1 user guide. 2004, Canberra: Centre for resource and environmental studies, The Australian National University.

[16] Topfer, F. and Pillewizer, W. The principles of selection, a means of cartographic generalization. Cartographic Journal [J]. 1966, 3(1): 10-16.

[17] Yang, Q. K., Guo, W. L., Zhang, H. M., et al. Method of extracting LS factor at watershed scale based on DEM. Bullet in of Soil and Water Conservation [J]. 2010, 30(2): 203-206, 211.

[18] Quinn, P., Beven, K., Chevallier, P., et al. The prediction of hillslope flow paths for distributed hydrological modelling using digital terrain models. Hydrological Processes [J]. 1991, 5(1): 59-79.