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Geomorphic Objects and Scale in Digital Terrain Analysis for Digital Soil Mapping

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15 Abstract — This paper presents our recent efforts on the two key 16 issues in digital terrain analysis for digital soil mapping: 17 quantification of spatial gradation of geomorphic objects and 18 scale of digital terrain analysis. Geomorphic objects (such as slope 19 positions, landform types) are rarely used as continuous variables 20 in digital soil mapping. We developed a framework for 21 characterizing and representing the spatial gradation of 22 geomorphic objects. This framework consists of two major 23 components: a fuzzy logic-based scheme for representing the 24 spatial gradation and a prototype-based technique for quantifying 25 the spatial gradation. Case studies in digital soil mapping have 26 shown that the framework is effective in quantifying the spatial 27 gradation of geomorphic objects. Our examination of scale in 28 digital terrain analysis for digital soil mapping focuses on the 29 following aspects: sensitivity analysis of computed terrain 30 attributes and digital soil mapping to neighborhood size, and the 31 relationship between neighborhood size and scale. Results show: 32 1) curvature measures are much more sensitive to neighborhood 33 size than slope gradient and that terrain variables are more 34 sensitive to neighborhood size at small neighborhood sizes than at 35 large neighborhood sizes; 2) neighborhood size of digital terrain 36 analysis has profound impact on the accuracy of digital soil 37 mapping and the most accurate soil map is not obtained at the 38 smallest neighborhood size; 3) There is no single spatial scale that 39 can be unambiguously associated with a given neighborhood size 40 and neighborhood size cannot be an adequate indicator of spatial 41 scale.

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INTRODUCTION

Topographic condition is one of the most important soil-44 forming factors [1]. The wide availability of digital terrain data 45 as well as the techniques for digitally deriving topographic 46 attributes [2] greatly facilitates the use of digital terrain 47 information in digital soil mapping. Among the studies in ⁴⁸ digital soil mapping examined by [3], about 80% of them ⁴⁹ employ topographic variables.

Two key issues in digital terrain analysis for digital soil 51 mapping are the quantification of spatial gradation of 52 geomorphic objects and scale of digital terrain analysis. Spatial 53 gradation of geomorphic objects refers to the transition of one 54 geomorphic object to another geomorphic object over space, 55 such as the transition from shoulder slope to back slope. 56 Information on this spatial gradation is rarely used because 57 geomorphic objects (such as slope positions, landform types) 58 are often considered as discrete, rather than continuous 59 variables in digital soil mapping and other geographic modeling 60 applications. Yet geographic processes over geomorphic objects 61 are often continuous and gradual rather than abrupt. For 62 example, soil erosion processes along a slope profile (from 63 should slope to back slope to toe slope) are continuous. 64 Furthermore, this spatial gradation of geographic processes 65 often cannot be captured by topographic attributes (such as 66 slope gradient) alone because topographic attributes contain 67 only local topographic information and usually describe the 68 geometric properties at a location on a terrain surface.

Examination of effect of spatial scale in digital analysis 70 has primarily focused on the effects of spatial resolution of 71 digital elevation model (DEM). Behrens et al.[4] and Smith et 72 al.[5] recently examined effect window size in digital soil 73 mapping. Their works show that the resolution of DEM is not 74 as important as the window (neighborhood) size over which 75 the terrain attributes are computed. Although these researches 76 have led to the conclusion that the resolution effects really the 77 manifestation of the effects of neighborhood sizes on terrain 78 attributes, another question needs examination, namely how 79 the effects of neighborhood size vary with the increase of

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⁸⁰ neighborhood size and how this neighborhood size related to ⁸¹ scale.

This paper presents our recent works on these two major sissues through three case studies. The first examines the quantification of spatial gradation of geomorphic objects and its feffects on digital soil mapping (Section 2). The second considers the effect of neighborhood size on digital soil mapping and the issues of relationship between neighborhood size and spatial scale (Section 3).

89 2. Spatial gradation of geomorphic objects

90 2.1 Quantification of spatial gradation

⁹¹ We believe that there are locations which capture (represent) ⁹² the central concept of a geomorphic object type (such as should ⁹³ slope) better than other locations. These locations are treated as ⁹⁴ prototypes for that geomorphic object type and their ⁹⁵ membership in that geomorphic object type is 1. The ⁹⁶ membership of other locations in the object type is determined ⁹⁷ by comparing these locations with the prototypes of that ⁹⁸ geomorphic object type. The more similar the locations to any ⁹⁹ of the prototypes, the high the membership they have. In this ¹⁰⁰ way, spatial gradation of geomorphic objects is captured and ¹⁰¹ quantified.

Based on the above idea, using slope positions as an 102 103 example we developed a prototype-based approach to quantify 104 the spatial gradation of geomorphic objects [6]. The approach 105 employs a two-tier hierarchical system of slope positions as a 106 basis for defining gradation among slope gradation. The first 107 tier considers the spatial context down the slope profile and 108 consists of five slope positions: ridge (summit), shoulder slope, 109 back slope, foot slope, and valley. The second tier is a 110 subdivision of three of the five first-tier slope positions 111 (shoulder slope, back slope, and foot slope) based on surface 112 curvature along the contour. They are further divided into 113 convex (or divergent), planar, or concave (or convergent) in 114 terms of contour curvature. Therefore, this slope position 115 system contains a total of eleven slope positions: ridge, 116 divergent shoulder slope, planar shoulder slope, convergent 117 shoulder slope, divergent back slope, planar back slope, 118 convergent back slope, divergent foot slope, planar foot slope, 119 convergent foot slope, and valley.

¹²⁰ In quantifying the spatial gradation of the slope positions, ¹²¹ this approach consists of two parts. The first is to extract the ¹²² prototypes for each slope position. The second is to compute the ¹²³ similarity between a given location and the prototypes of slope ¹²⁴ positions based on both the local topographic attributes and ¹²⁵ spatial context.

126 2.2 Effect on digital soil mapping

¹²⁷ A case study was used to examine the usefulness of ¹²⁸ information on spatial gradation of slope positions for mapping ¹²⁹ soil organic matter content. The study area consists of two ¹³⁰ portions: One is about 4 km² used for model development; and ¹³¹ the other is about 60 km² used for model extrapolation. The ¹³² results of the evaluation show that the model based on the ¹³³ quantified spatial gradation predicts the SOM better than a ¹³⁴ multiple linear regression model (MLR) using topographic ¹³⁵ variables (Table 1). In addition, the information on spatial ¹³⁶ gradation of geomorphic objects can help us to identify where ¹³⁷ representative samples should be collected. Results in the ¹³⁸ model-development area show that the performance of the ¹³⁹ spatial gradation based model with 5 modelling points is ¹⁴⁰ comparable to that of the MLR developed with 48 points.

141 Table 1: Evaluation of predicted soil organic matter content 142 in the top layer

Model	CC*	RMSE	Sample Used	Validation Points
Gradation	0.319	1.31	5	102
MLR	0.056	1.49	48	102

¹⁴³ * CC: Correlation Coefficient

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3. SCALE OF DIGITAL TERRAIN ANALYSIS

145 3.1 Effects of neighborhood size

¹⁴⁶ In this case study we examine effects of neighborhood size ¹⁴⁷ in two ways: 1) the sensitivity of terrain attributes to ¹⁴⁸ neighborhood size and 2) the impact of neighborhood size on ¹⁴⁹ accuracy of digital soil mapping.

We employed four basic terrain attributes (slope gradient, 151 profile curvature, contour curvature) for examining the 152 sensitivity of the terrain attribute values to the neighborhood 153 size over which these attribute values were computed [7]. Fig. 1 154 shows the "relative change" across neighborhood. The "relative 155 change" concept measures the difference in deviation from the 156 mean between two consecutive neighborhood sizes at a point. It 157 therefore provides a way to characterize the sensitivity across 158 neighborhood size and it allows us to identify neighborhood 159 sizes to which the terrain conditions are more or most sensitive. 160 The results show that curvature measures are much more 161 sensitive to neighborhood size than slope gradient and that 162 terrain variables are more sensitive to neighborhood size at 163 small neighborhood sizes than at large neighborhood sizes.



¹⁶⁵ Figure 1: Relative change of deviation from the mean between ¹⁶⁶ two consecutive neighborhood sizes.

167 3.2 Effect on digital soil mapping

Effects of spatial processes on geographic patterns and vice teg versa manifest itself over a certain area. The interaction of tro geographic factors is a process of exchanging energy and matter train and this exchange requires spatial extent (or a neighborhood) to train this exchange requires spatial extent (or a neighborhood) to train neighborhood". Topography, as an important factor controlling train the redistribution of energy and matter at local level, plays a key train of energy and matter at local level, plays a key train are not purely dependent on the topographic conditions at this train point but rather dependent on the topographic train conditions over a certain area around this point because the train redistribution of energy and matter needs an area of certain size to play out. We certainly expect that effective neighborhoods the are different for different spatial processes.

¹⁸² Under the above notion, the assumption, that the accuracy of ¹⁸³ digital soil mapping will increase simply as the resolution of ¹⁸⁴ spatial data increases or the neighborhood size used decreases, ¹⁸⁵ may not always hold. Here we are trying to show how the ¹⁸⁶ impact of neighborhood size on digital soil mapping varies over ¹⁸⁷ a range of neighborhood sizes [5].

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¹⁹⁹ resolution, we obtain a version of the soil map using the SoLIM ²⁰⁰ approach based on terrain derivatives that have been generalized ²⁰¹ at that neighborhood size. The range of neighborhood sizes we ²⁰² employed in this study is from 10 ft to 180 ft for DEM ²⁰³ resolutions of 10 ft, 15 ft, and 30 ft. Field soil samples were ²⁰⁴ collected to assess the accuracy of predicted soil map at each ²⁰⁵ neighborhood size.

Fig. 2 shows the variation in accuracy of predicted soil map Proference in 2007 and neighborhood size. It is clear that neighborhood size has Profound impact on the accuracy of soil map. The difference in Profound impact on the accuracy of soil map. The difference in Profound impact on the accuracy of soil map. The difference in Profound impact on the accuracy at one neighborhood size can be quite Profound in the accuracy at one neighborhood size perhaps Profound that at another neighborhood size. It is important to Profound that the most accurate soil map is not obtained at the Profound the most accurate soil map is not obtained at the Profound the most accurate sole but at some particular neighborhood Profound Profound 100 feet in this particularly case study). The Profound in DEM is profound for digital soil mapping because Profound the scale details do not contribute to the differentiation of Profound at the scale interested by the soil scientists.

The combination of what presented in 3.1 and what in this 220 section makes a strong argument against the use of small 221 neighborhood size in digital soil mapping because of the high 222 sensitivity of terrain attributes to small neighborhood size and 223 the effective neighborhood. This argument is of particular 224 importance today when finer and finer DEM data are produced 225 with the rapid deployment of Lidar for acquiring high resolution 226 digital elevation data.

227 3.3Neighborhood size and spatial scale

Spatial scale is a fundamental issue in many geographic analyses [9][10][11][12][13]. Depending on the context, spatial scale could mean the followings: grain and extent [10][14][15] [16]. Grain refers to the spatial detail or the minimum areal unit spatial resolution which refers to the spatial detail or the spatial unit over which a particular process should be studied. Grain is not spatial resolution which refers to the spatial detail or the spatial to ver which spatial data are collected and/or represented. There is no necessary connection between grain size mentioned above and spatial resolution because the spatial detail at which spatial data are captured or represented may not be the spatial detail at which a given spatial process needs to be studied. Extent refers to the size of the study area.

In this paper spatial scale refers to "grain size". In other words, by 'spatial scale' we mean the size of a given feature or minimal area needed for a process to manifest itself. Note that scale' is defined as in earth sciences and physical keineces, e.g. the characteristic length scale in the turbulence theory, but not in cartography, where 'scale' is the ratio of map where 'scale' is defined as a rill might where the spatial scale of a rill might where the spatial scale of a hill could be 200m or more.

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²⁴⁸ Typical landscapes contain multiple scales, but for a particular ²⁴⁹ application only some scales are relevant. Ideal terrain ²⁵⁰ characterization (such as slope computation) would capture ²⁵¹ those and ignore the others.

²⁵² "Neighborhood size" is often treated as the "spatial scale" of ²⁵³ computation in digital terrain analysis, just as we have done ²⁵⁴ above, but are they the same? If not, is 'neighborhood size' an ²⁵⁵ adequate indicator of 'spatial scale'? Using rater-based slope ²⁵⁶ estimation as example with amplitude response functions as the ²⁵⁷ measure we analytically examine these questions.

As is well-known, a DEM can be represented using a discrete Fourier series, which decomposes the surface into a finite number of sinusoids of progressively shorter wavelength. Any particular slope calculation will treat information at various scales differently, suppressing some frequencies, amplifying others, and leaving the rest untouched. Therefore, a slope det operator is like a digital filter of the input DEM and the 'spatial scale' of a slope calculation refers to the frequencies that pass the filter and are reflected in the resulting slope matrix.

Table 2 compares the frequency of neighborhood size along 268 the $f_x = f_y$ transects of the amplitude response surfaces of the 269 slope estimators examined. As shown in Table 2, none of the 270 analyzed slope estimators has the neighborhood size fall into a 271 major passing band(s). Therefore, the neighborhood size and 272 the spatial scale are not numerically the same. It is also 273 important to note that neighborhood size corresponds to only 274 one frequency/scale, while all the frequencies/scales that fall 275 into the passing band(s) are part of the 'scale' of the slope 276 estimator. Thus there is no single scale that can be associated 277 with an estimator.

Through this case study, we hoped to shed some light on the perfects of scale on digital terrain analysis and digital soil analysis and digital soil mapping are clear but neighborhood size is not space scale. The question remains as to what the neighborhood size is appropriate for a given scale of analysis.

Table 2: Comparison of neighborhood size and spatial scale

Method	f of neighborhood size	Peak passing f	
Horn (1981)	0.333 for 3*3	0.168	
Evans(1979)	0.033 for 3*3	0.149	
Wood (1996)	0.2 for 5*5	0.085	
Wood (1996)	0.14 for 7*7	0.06	

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